

CHAPTER 1

INTRODUCTION

1.1 Liquid Crystals

During the process of melting, certain organic crystals pass through one or more turbid, fluid phases, before they transform to a clear isotropic liquid. This was first discovered by Reinitzer in 1888.¹ Such intermediate phases possess liquid like properties such as viscosity and surface tension. At the same time, they exhibit many crystalline properties, i.e., optical birefringence, dielectric and diamagnetic anisotropies, etc. As their physical properties are intermediate between those of crystals and liquids, such phases are called liquid crystals or mesophases,

The molecular ordering in liquid crystals differs from normal crystals, in which there is long range 3-dimensional positional ordering, and from isotropic liquid in which no long range correlations of any nature exist. The ordering in liquid crystals is only partial and it may be positional, orientational or both.

Two major categories of liquid crystals are known. Thermotropic liquid crystals are those in which the

mesophase is brought about by the action of heat on the crystalline solid. Lyotropic mesophases are obtained, on the other hand, by dissolving the material in suitable solvents. When the concentration exceeds a critical value, the solute molecules tend to become aligned, thus giving rise to the mesophases. This thesis is concerned only with thermotropic liquid crystals.

Based on the nature of the molecular ordering they exhibit, liquid crystals have been divided² into three major classes: nematics, cholesterics and smectics.

(a) Nematic liquid crystals: Nematics are characterized by a high degree of long range orientational ordering, but they possess no long range translational ordering. The long axes of the molecules have a tendency to align themselves parallel to each other (Fig. 1.1a). The unit vector, \hat{n}^A , along the average direction of alignment is called the director. Experiments show that \hat{n}^A and $-\hat{n}^A$ are equivalent and hence \hat{n}^A is apolar. The nematic phase is optically uniaxial and strongly birefringent.

(b) Cholesteric liquid crystals: Cholesteric liquid crystals are nematic type of liquid crystals with the difference that the molecules are optically active. The director, $\hat{n}^A(n_x, n_y, n_z)$ as a consequence, follows a helix (Fig. 1.1b) of the form

$$\begin{aligned}n_x &= \cos(q_0 z + \varphi) \\n_y &= \sin(q_0 z + \varphi) \\n_z &= 0\end{aligned}$$

where a is the direction of the axis of the helix and φ is a phase angle. The structure is periodic with a spatial period $L = \pi/q_0$. When L corresponds to the wavelength of visible light, they are found to reflect the light strongly in a Bragg like manner.

(c) Smectic liquid crystals. The smectic mesophase has a layered structure. The interlayer coupling is weak enough to allow the layers to slide past each other, thus giving rise to the fluidity. The various possible molecular arrangements within a layer give rise to the different smectic modifications.

In the smectic A phase, the molecules within each layer have a long range orientational ordering, but no long range positional ordering (Fig. 1.1c). The director is parallel to the layer normal. There is an infinite fold symmetry axis normal to the layers and this leads to the uniaxial character of this phase.

The smectic C phase is similar to the smectic A except that the molecules within the layers are tilted with respect to the layer normal (Fig. 1.1d). This phase is optically biaxial. The angle of tilt may remain constant or it may

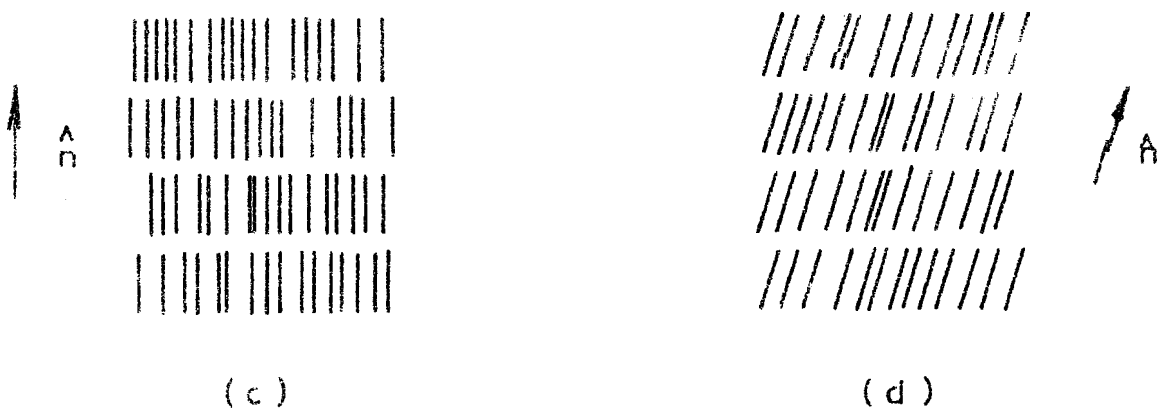
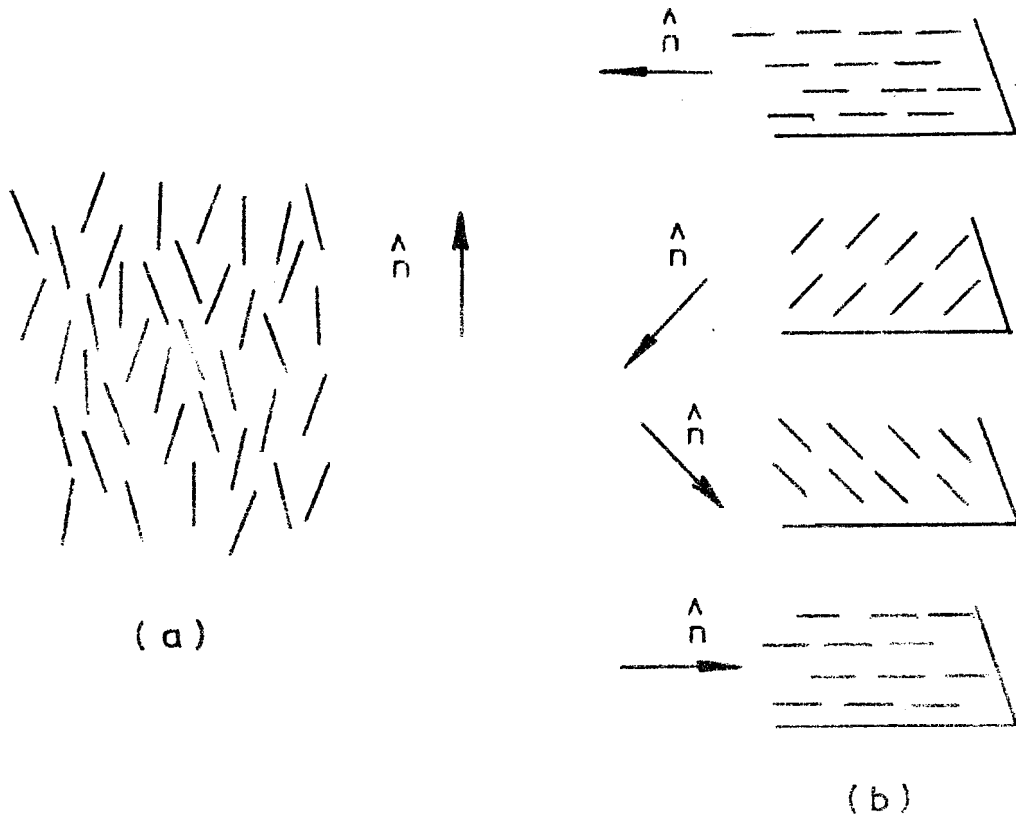


Figure 1.1

Schematic representation of the molecular order in some liquid crystals. (a) Nematic (b) Cholesteric (c) Smectic A (d) Smectic B.

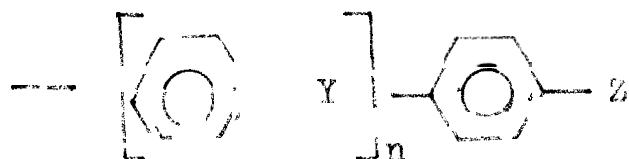
vary with temperature.^{3,4}

In the smectic B and H phases, the molecules are arranged in a hexagonal lattice within the layers. Hence, these layers possess a two dimensional positional ordering. In the B phase, the director is parallel to the layer normal, whereas in the H phase it is tilted.

Other smectic modifications, labeled E, F, G, etc. have been discovered in recent years. Their detailed structure is yet to be understood completely.

Some materials exhibit only one mesophase between the solid and Isotropic phases, while some others exhibit more than one. The latter type are said to be polymesomorphic. Mesophases which occur during both heating and cooling are known as enantiotropic, while those that appear only on cooling are termed monotropic.

An essential requirement for the formation of mesophases is that the shape of the molecules should be highly anisotropic. Nematic and smectic behaviour is generally observed in materials having the schematic structure



where X and Z are end groups, typically alkyl, alkoxy,

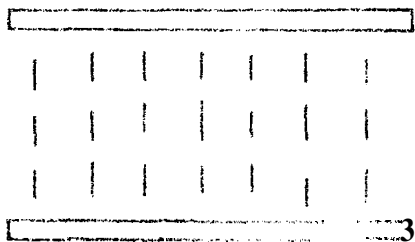
cyano, etc. and Y is a linkage group which is typically azo, azoxy, azomethine, ester, etc. and $n = 0, 1, 2$. In some cases, as in 4'-n-alkyl-4-cyanobiphenyls, no linkage group may be present at all. Cholesteric liquid crystals are usually obtained from optically active derivatives of cholesterol.

When a liquid crystalline sample is contained between two untreated glass plates of a cell, a large number of domains can be observed. Each domain is well ordered within itself, but the directors of the different domains are arranged in a random manner. The domains can be aligned in a common direction using relatively low electric and magnetic fields. It is also possible to accomplish this through appropriate treatment of the substrate surfaces. Depending on whether the molecules are parallel or perpendicular to the walls, of the cell, the alignment is referred to as 'homogeneous' or 'homoeotropic' respectively (Fig. 1.2).

The anisotropic nature of the mesophases gives rise to several interesting physical properties such as curvature elasticity, anisotropic viscosity, etc., but we shall not be concerned with those aspects of the subject. They have been dealt with extensively in a number of recent reviews and monographs.⁵ We shall confine our attention in this thesis primarily to the applications of infrared techniques to the study of thermotropic liquid crystals.



(a) HOMOGENEOUS



(b) HOMEOTROPIC

Figure 1.2

Schematic representations of (a) homogeneous alignment (b) homeotropic alignment.

1.2 Vibrational Spectra of Liquid Crystals

The degrees of freedom available to the molecules in the different types of mesophases has been a topic of considerable interest both from the experimental and theoretical standpoint. Experiments show that in the uniaxial nematic and smectic A phases, the molecules rotate nearly freely about their long axes,^{6-8,12} Theoretical models of the more ordered smectic C and smectic H phases presume that in these phases such rotation is absent.⁹⁻¹¹ However recent experiments do not support this view^{7,12,13}, in fact the neutron scattering experiments¹³ seem to show that body reorientations of the molecules about their long axes can occur even in a smectic H phase with a correlation time $\sim 18 \times 10^{-12}$ sec. Also, the dynamics of the alkyl end chains of mesogenic molecules is another important factor in determining the nature of molecular ordering in liquid crystals. This has been demonstrated by recent experimental¹⁴ and theoretical¹⁵⁻¹⁷ work. In this respect, possible conformational changes that can occur in the end chains in the different mesophases as also at the crystal-liquid crystal transition are of particular interest and several studies have been carried out in this direction,¹⁸⁻²² Marked pretransition phenomena have also been reported in some cases in the behaviour of the crystalline solid in a temperature interval just

preceding the crystal-mesophase transition.^{19,23-25}
 These changes were attributed to the occurrence of increased molecular motion which 'prepares' the crystal for the transition to the mesophases.

From the foregoing remarks it is evident that the study of intra and intermolecular vibrations in the different phases of mesogens is of considerable importance. The vibrational spectra of several liquid crystals have been studied from this view point using infrared and Raman spectroscopic methods,²⁶⁻²⁸ but as liquid crystalline systems are rather complex, the answers to many of the problems touched upon in the preceding paragraph are by no means unequivocal. The present study was undertaken with a view to throwing further light on some of these and other related problems. We begin with a brief review of the underlying principles of vibrational spectroscopy. According to classical theory, a modulated component of the dipole moment of a physical system will lead to the emission or absorption of radiation. If the initial state of the system is described by the wave function ψ_i and the final state by ψ_f , then absorption or re-emission of radiation can occur during this transition only if the matrix element

$$\langle \psi_f | \mu | \psi_i \rangle \neq 0 ;$$

here μ is the dipole moment of the system. Only the creation or annihilation of a single photon is involved in this process. On the other hand, Raman scattering is the inelastic scattering of photons by excitations in any medium. An incident photon is destroyed in this case, and a scattered photon emerges with a different energy, the difference in energy corresponding to a characteristic quantum of excitation of the system. For such a process to occur, the appropriate condition is that

$$\langle \psi_f | \alpha | \psi_i \rangle \neq 0 ,$$

where α is the polarizability tensor of the system. Classically, Raman scattering can occur only when a time-varying component of the polarizability tensor exists in the system. The physical origins of infrared absorption and Raman scattering being different, the two spectra often yield complementary information. In particular, for systems which possess a centre of inversion, the two spectra are mutually exclusive and both are needed to obtain a more complete picture of the vibrational spectrum.²⁹

A free polyatomic, geometrically non-linear molecule containing N atoms would possess $3N-6$ intramolecular normal modes. Based on the symmetry of the molecule, group theory enables one to classify these normal modes according to the different irreducible representations of the point group of

the molecule. Such a classification is also useful in predicting the number of infrared and Raman active modes. Specifically, if at least one component of the dipole moment transforms according to the irreducible representation of a given normal mode, that mode will be active in the infrared spectrum. Similarly, the mode will be Raman active only if its representation is contained in the reduction of the representation corresponding to that of the polarizability tensor.²⁹

In the case of complex organic molecules, the large number of atoms and the low symmetry of the molecules can complicate the interpretation of the spectra. However, systematic studies on a large number of chemically related systems have led to the identification of 'group frequencies', i.e., the frequencies corresponding to the vibrations of specific pairs or groups of atoms. Such data are often useful in interpreting a given spectrum and in obtaining structural information about the molecule. The group vibrations which involve pairs of atoms or small groups of them, normally occur in the high frequency region, between 650 cm^{-1} and 3500 cm^{-1} . Hence, this region is often referred to as the 'fingerprint' region of the spectrum. The group vibrations of still larger clusters of atoms, as exist in mesogenic molecules, may be observed at much lower frequencies. While relying on group frequencies to

interpret the spectra of complex molecules, due caution must be exercised as the group vibrations may not necessarily correspond to the normal modes of the molecule.

Detailed studies of low frequency intermolecular vibrational modes in mesogens has been attempted only since the last ten years. The progress made in this direction is undoubtedly due to the increased availability of improved experimental techniques and spectrometers. Historically, infrared spectra were difficult to obtain in the region below $\sim 250 \text{ cm}^{-1}$, mainly due to the lack of strong sources of radiation and sensitive detectors. The use of dispersive spectrometers in this region only aggravates the problem as they are inherently wasteful of radiation and hence yield spectra with poor signal-to-noise ratio. The development of commercial far-infrared Fourier spectrometers during the last 10 years has contributed vastly to the relative ease and accuracy with which far-infrared spectra can be obtained now-a-days. All the low frequency infrared spectra reported in this thesis were measured using the Yolytec far-infrared Fourier spectrometer. Near-infrared spectra are relatively easy to obtain with conventional dispersive instruments and a Leitz double-beam spectrograph was used to obtain such spectra. The details of these instruments and the experimental techniques employed during the work reported in this thesis are discussed in chapter 2.

Organic materials often exhibit solid state polymorphism and this is true of many mesogens too.³⁰⁻³⁴ However, these transitions acquire, particular importance! in mesogenic materials because the changes in the solid phase may reflect an anticipation of the formation of the mesophase. X-ray structural data on the solid phases of p-azoxyanisole (PAA) and p-azoxyphenetole (PAP) show that *the* molecules are arranged with their long axes nearly parallel to each other in an imbricated structure*³⁵ Such an arrangement in a less ordered fashion, with the molecules acquiring translational freedom along their long axes, could lead to the formation of the nematic phase. Recent studies on cholesteryl esters show that slightly below the transition to the mesophase, the crystalline order decreases markedly in directions normal to the long axes of the molecules.²³ This was interpreted as an anticipation of the transition to the mesophase which, of course, exhibits complete disorder in directions normal to the long axes of the molecules. From neutron scattering and infrared studies of the solid phases of PAA and p-methoxybenzylidene-p'-n-butylaniline (MBBA), the existence of a 'soft solid' region below the nematic transition temperature has also been suggested.^{24, 32, 36}

A crystalline solid exhibits characteristic external or lattice modes which arise due to the coupled rigid body

rotations and translations of the molecules within a unit cell. These modes, which are of low frequency, are therefore sensitive to the crystal structure. Hence, in the case of pre-transition effects in the solid phase, where the molecules are thought to acquire greater motional freedom, or in polymorphic transitions, where the crystal structure undergoes an abrupt change, it can be expected that these external modes should exhibit striking changes.

In chapter 3, we discuss the results of a study of the temperature dependence of the far-infrared and Raman spectra of the crystalline phase of *n*-*p*-cyanobenzylidene-*p*-*n*-octyloxyaniline (CBOOA). This study reveals the existence of a solid-solid transition 8°C below the solid-smectic A transition. We have confirmed this transition using differential scanning calorimetry. We have also studied the X-ray powder diffraction patterns of these two phases. These show that the crystal structures are different in the two phases. We also discuss the implications of this transition to the occurrence of the mesophase.

In a crystalline solid, wave vector conservation dictates that in a first order vibrational spectrum, only those modes can participate whose wave vector is nearly zero. Such optical modes lie close to the centre of the Brillouin zone of the crystal and are hence referred to as zone-centre modes. For these modes, the characteristic

atomic motions are in phase over a very large number of unit cells within the crystal. Thus, translation can be considered to be the identity element. In order to determine the number of vibrational modes in a first order spectrum and the irreducible representations to which they belong, it is hence sufficient; to consider only the point group symmetry of the crystal and examine the behaviour of the atoms within the primitive cell. This is easily accomplished using straightforward group-theoretical methods.^{29,37,38} Further, when one is only concerned with the external modes, it is sufficient to regard the molecules as rigid units. Then the number and site symmetry of the molecules within the primitive cell is ²¹¹ the information needed for determining group theoretically the number of external modes and the irreducible representations to which they belong. A group theoretical analysis of the external modes of CBOOA and terephthal-bis-butylaniline (TBBA) *have* been carried out and this is discussed in Appendix A.

In chapter 4 we discuss the results of a near and far-infrared spectroscopic study of the phase transitions in CBOOA. We have obtained evidence for conformational changes in the alkyl end chain at the crystal-smectic A transition. We also present the results of a dichroism study in the near and far-infrared regions. *representative*

assignments have also been made for many of the observed bands.

The lineshape of vibrational bands and their accompanying changes at the different transitions exhibited by mesogens deserve a careful analysis. It is well known that such information can provide much insight into the dynamics of inter and intramolecular motion.³⁹ The nature of molecular motion is clearly influenced by the local ordering and environment of the molecules and this varies considerably within the many different types of mesophases that are now known to exist. In recent years neutron scattering^{13,24} and NMR⁷ have emerged as especially powerful methods for such studies on mesogens. However, these techniques are quite often limited in their ability to probe, in detail, any molecular motion which occurs on a time scale faster than 10^{-11} sec. On the other hand, the infrared and Raman spectra of these systems are potentially capable of discerning molecular rotations or reorientations which occur at much higher frequencies. Despite this advantage, systematic and detailed studies on vibrational bandshapes of mesogens have remained quite scarce so far.^{40,41} The rather rich vibrational spectra of mesogens and the consequent difficulty of making unambiguous assignments to the observed bands are perhaps the major reasons for this situation. Nevertheless, such investigations

would be interesting, especially in the case of poly-mesomorphic materials. For this reason, we carried out lineshape studies on an absorption band of TBBA and this has enabled the determination of correlation times characteristic of intramolecular reorientations in the highly ordered smectic phases of this mesogen. These results are discussed in chapter 5.

A useful measure of the long range orientational ordering is the parameter, S , defined as

$$S = \langle P_2(\cos \theta) \rangle = \frac{1}{2}[3 \langle \cos^2 \theta \rangle - 1]$$

where θ is the deviation of the long axis of the molecule from the average direction of orientation and P_2 is the second Legendre polynomial. The angular brackets denote a statistical average over all molecules in the medium. For perfect ordering $S = 1$ and for complete disorder $S = 0$.

It is of interest to consider the temperature variation of S . This has been measured in nematic and smectic A liquid crystals using a number of techniques.⁴²⁻⁵² Most infrared studies performed hitherto to measure the orientational order parameter have used homogeneously aligned samples and polarized radiation. The need for polarized radiation and the consequent reduction in available energy are two of the inherent disadvantages of this method.

In contrast, a homeotropically aligned sample facilitates the use of unpolarized radiation.⁵³ This method also possesses other distinct advantages; consequently we have it in all our measurements of the orientational ordering in the smectic A and nematic phases of liquid crystals. In chapter 6, we discuss this method and apply it to determine the orientational ordering in CBOOA. The results of our investigations are found to agree well with some of the earlier studies of the orientational order parameter in this material.

The temperature and entropy of the nematic-isotropic transition as well as the order parameter at the transition are known to exhibit an alternating behaviour as a homologous series is ascended.¹⁴ Recent theoretical work¹⁵⁻¹⁷ has shown that the nature of the conformations adopted by the hydrocarbon end-chains is primarily responsible for this behaviour. In chapter 7, we discuss the results of our study of the orientational order parameter in the smectic A and nematic phases of some members of the homologous series, trans-p-n-alkoxy- α -methyl p'-cyanophenyl cinnamates (n-OMCPC). The order parameter discontinuities at the smectic A-nematic transition in some of the higher homologues of this series have also been measured and correlated with their thermodynamic properties. Calorimetric evidence for tricritical behaviour of the smectic A-nematic transition in mixtures

of these compounds are also presented in this chapter.

A novel differential technique has "been developed in the course of the present study for obtaining the dichroic spectra of uniaxial liquid crystals from a single spectral scan, using unpolarized radiation. The differential technique is equally applicable to the study of anisotropic solute molecules which can be aligned in a liquid crystalline solvent. These aspects of differential dichroic spectroscopy with illustrative results are presented in chapter 8.

Some of the results discussed in this thesis are reported in the following publications:

1. Far-Infrared and Raman Spectra of the Solid Phases of CBOOA (S. Venugopalan, J.R. Fernandes and G.V.Vani) - MOLECULAR CRYSTALS AND LIQUID CRYSTALS 31, 29-46 (1975).
2. Infrared Spectroscopic Study of Orientational Order and Phase Transformations in Liquid Crystalline CBOOA (J.R. Fernandes and S. Venugopalan) - MOLECULAR CRYSTALS AND LIQUID CRYSTALS 35, 113-134 (1976).
3. Far-Infrared Absorption in the Highly Ordered Smectic Phases of TBBA (S.Venugopalan, J.R.Fernandes and V. Surendranath) - MOLECULAR CRYSTALS AND LIQUID CRYSTALS 40, 149-161 (1977).
4. Differential Dichroic Spectroscopy in Liquid Crystals Using Unpolarized Radiation (J.R.Fernandes and S.Venugopalan) CHEMICAL PHYSICS LETTERS 53, 407 (1978).

5. **Orientational Order and Tricritical Behaviour in the trans-p-n-Alkoxy- α -Methyl p'-Cyanophenyl Cinnamate (n-OMCPC) Series of Liquid Crystals (J.R.Fernandes and S. Venugopalan)(to be submitted).**

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