

## CHAPTER 1

### WATER VAPOUR IN THE ATMOSPHERE - A BRIEF REVIEW

#### 1.1 Introduction

Water vapour, although it constitutes less than 3 percent by volume of the atmosphere, even at sea level with moist conditions, is the most important variable gas in the atmosphere. It absorbs nearly six times as much solar radiant energy as all the other gases combined and accounts for nearly all of the gaseous absorption of terrestrial radiation. With the liquid water and ice particles suspended in the atmosphere, water vapour plays a predominant role not only in the radiation balance but in the whole mechanism of heat transfer in the atmosphere.

Equally important are the thermodynamic effects of water vapour in its role of dew, frost, cloud, fog and precipitation formation, which are responsible for what we all call weather. The measurement of the water vapour content of the atmosphere and an understanding of its thermodynamic effects is therefore of vital concern to meteorologists and hydrologists. It plays a crucial role in the dynamics of the atmosphere, because it is a source of atmospheric energy and its presence affects the release and transformation of both elec-

trical and thermal energy, being the origin of all hydrometeors and the main absorber in the lower atmosphere of **infra-red** radiation. In addition, the water vapour content of the air can be used as a natural tracer, both horizontally and vertically, in meteorological studies.

In the infrared and far infrared, water vapour is a selective absorber, absorbing almost totally at wavelengths greater than  $27\ \mu$  and between  $5.5$  and  $7\ \mu$ . It has also a few narrow absorption bands below  $4\ \mu$  and absorbs moderately from  $4$  to  $5.5\ \mu$ ,  $7$  to  $8\ \mu$  and  $13$  to  $27\ \mu$ . However, for wavelengths from  $8$  to  $13\ \mu$ , it is almost perfectly transparent. Recent precise determinations of water vapour absorption in most regions of the solar and terrestrial radiation spectra (Fig 1.1) have given a fairly complete picture of the absorption by water vapour in the various regions of the solar spectrum (Valley, 1965).

Water vapour in the atmosphere varies widely with time and locality and with height in the atmosphere. Though most of the water vapour is confined to the lower troposphere, measurable amounts have also been detected in the stratosphere up to **30 km**.

The maximum amount of water vapour which the

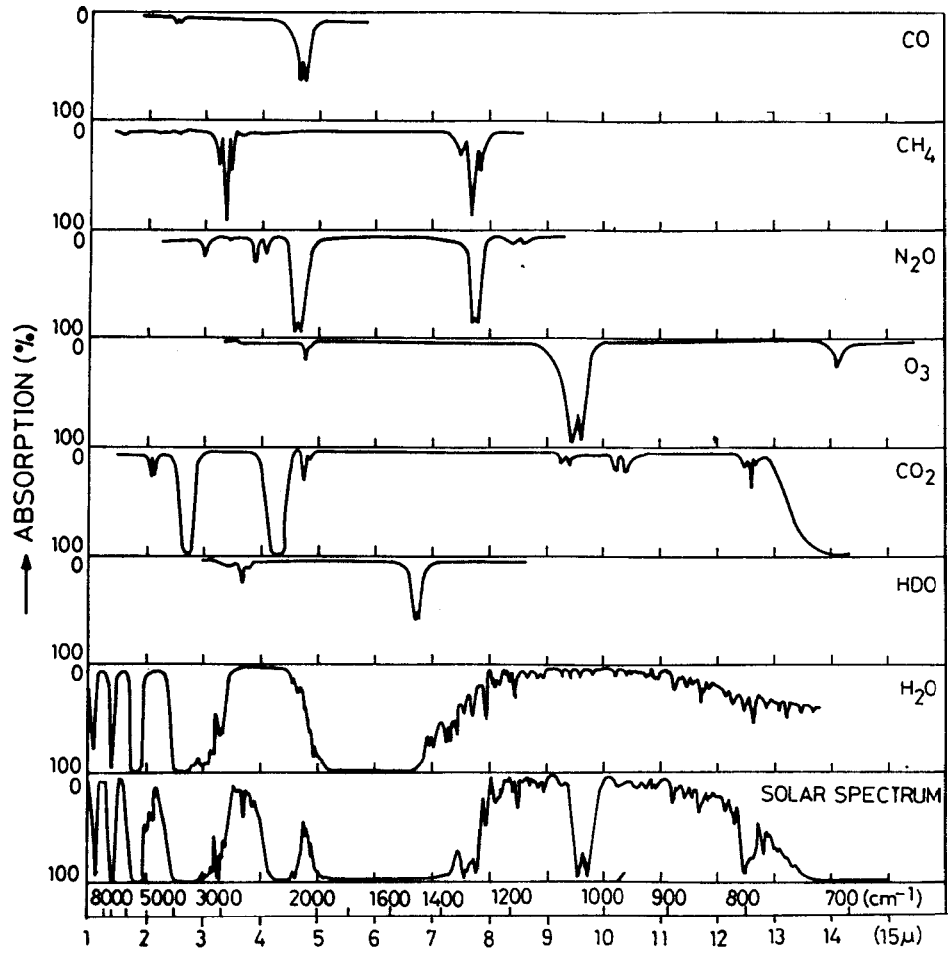


Fig 1.1 Water vapour absorption in the various regions of solar and terrestrial radiation spectra.

**atmosphere** can contain is regulated by **its** temperature. For **example**, at the highest recorded station temperature of about  $55^{\circ}\text{C}$ , the air can **hold** about  $100 \text{ g m}^{-3}$ . The amount **actually** present in the atmosphere is a **complex** function of various weather parameters. The highest water **vapour** content recorded is about  $30 \text{ g m}^{-3}$ , corresponding to a dew point of **approximately**  $30^{\circ}\text{C}$ . As the temperature decreases, the amount of water vapour the air contains decreases **rapidly**, approaching a **negligible** amount at temperatures **below**  $-40^{\circ}\text{C}$  to  $-50^{\circ}\text{C}$ . At these **low** temperatures, the amount of water vapour the air can contain at the surface is  $10^{-1}$  and  $4 \times 10^{-2} \text{ g m}^{-3}$ , **respectively**. **Although** the water vapour content at temperatures **below**  $-40^{\circ}\text{C}$  is **extremely small**, even this amount is **important** in the transmission of infrared **radiation** over long path **lengths** (Wolfe, 1965).

## 1.2 Terminology and Units of Measurement

1.2.1 **Fundamentally, all** measurements of water vapour or atmospheric humidity are based on quantities **related** to evaporation and condensation over a **flat** surface of pure water. From a water surface that is evaporating, the excess of **molecules** of water **leaving** the surface,

over those coming back, is expressed and measured as a pressure. This pressure depends only on the temperature of the water surface. If the quantity of water vapour present does not vary by either addition by evaporation or removal by condensation, the vapour pressure will remain constant, provided the total pressure of all the gases does not change.

1.2.2 The ways in which water **vapour** in the atmosphere can be specified are many and varied. The terminology used in **this** study follows the official definitions and specifications of the parameters of water vapour laid down by the World Meteorological Organization (1971). The units normally used for expressing the various quantities associated with water vapour in the atmosphere are:

- (i) Vapour pressure, in millibars,
- (ii) Density of water vapour or absolute humidity, in  $\text{g/cm}^3$  or  $\text{g/m}^3$ ,
- (iii)** Moisture content or specific humidity, **in g/kg,**
- (iv) Mixing ratio, in  $\text{g/kg}$ , and
- (v) Relative humidity, in per cent.

The terms and units used are described in detail below.

1.2.2.1 Vapour pressure,  $e$ , of water vapour in moist air at total **pressure**  $p$  and with mixing ratio  $r$ , **is** defined by  $e = \frac{r}{0.622 + r} \cdot p$  and is an absolute measure of the quantity of water vapour present.

1.2.2.2 saturation vapour pressure,  $e_w$ , of pure aqueous water vapour with respect to water, is defined as the pressure of the vapour when in a state of neutral equilibrium with a plane surface of pure water at the same temperature and pressure. Similarly  $e_i$  is saturation vapour pressure over ice. Both vary with temperature so that the higher the temperature, the greater the vapour pressure required for saturation. It is again expressed **in** millibars.

1.2.2.3 Relative humidity,  $U_w$ , with respect to water, of moist air at pressure  $p$  and temperature  $T$ , is the ratio in per cent of the two vapour **pressures**, the actual and the **saturation** vapour pressure. The actual vapour pressure changes with atmospheric pressure and the saturation vapour pressure with temperature.

It is expressed as:

$$U_w = 100 \left( \frac{e}{e_w} \right) \quad (1.1)$$

1.2.2.4 Density or concentration of water vapour or absolute humidity,  $d_v$ , is the amount of moisture contained in a unit volume and is usually expressed in  $\text{g/cm}^3$  or  $\text{g/m}^3$ . It is defined as the ratio of the mass vapour  $m_v$  to the volume  $V$  occupied by the mixture:

$$d_v = \frac{m_v}{V} \quad (1.2)$$

1.2.2.5 Moisture content or masa concentration or specific humidity,  $q$ , of moist air, is defined as the ratio of the mass  $m_v$  of water vapour to the mass ( $m_v + m_a$ ) of moist air, in which the masa of water vapour  $m_v$  is contained:

$$q = \frac{m_v}{m_v + m_a} \quad (1.3)$$

Now  $m_v = d_v \cdot V$  and  $m_a = d_a \cdot V$ ,

As the  $V$ 's cancel, we have

$$q = \frac{d_v}{d_a + d_v} \quad (1.4)$$

the denominator being the total density of the dry air,  $\rho_a$ , plus that of the water vapour  $\rho_v$ .

1.2.2.6 The mixing ratio,  $r$ , is defined as the ratio of the mass  $m_v$  of water vapour to the mass  $m_a$  of **dry** air, with which the water vapour is associated.

$$r = \frac{m_v}{m_a} \quad (1.5)$$

It differs from specific humidity only in that it is related to dry air instead of the total of dry air plus water vapour.

1.2.2.7 The dew and frost point temperature,  $T_d$  and  $T_f$ , of moist air at pressure  $p$  and mixing ratio  $r$ , are the temperatures at which moist air, saturated with respect to water or **ice** at the given pressure, has a saturation mixing ratio  $r_w$  equal to the given mixing ratio  $r$ . In saturated conditions, the dew point/frost point and air temperatures are equal.

1.2.2.8 Equation for water vapour

As long as no condensation or fusion is taking place, water vapour may be treated as an ideal gas. For an ideal gas, the following relation exists



between pressure  $p$ , density  $\rho$  and absolute temperature  $T$ .

$$p = \frac{R^*}{m} \cdot \rho \cdot T. \quad (1.6)$$

where  $R^*$  is the universal gas constant and equals  $83.12 \times 10^6$  ergs/gm degree or 1.986 cal/gm degree and  $m$  is the molecular weight of gas. If  $e$  is the water vapour pressure and  $M_w$  is the molecular weight of water (18),  $d_v$  its density and  $T$  its temperature and  $M_a$  the molecular weight of dry air = 28.9,

$$d_v = \frac{e}{R^* T} \cdot M_w = \frac{M_w}{M_a} \cdot \frac{e}{RT} \quad (1.7)$$

where  $M_w/M_a = 0.622$  and  $R = R^*/M_a$  is the gas constant for dry air,

$$d_v = 0.622 \cdot \frac{e}{RT} \quad (1.8)$$

The total density of the moist air  $\rho$  is the sum of the density of dry air and of water vapour.

The partial pressure of dry air is  $p-e$ , where  $p$  is the total pressure of moist air. Consequently

$$\begin{aligned} \rho &= \frac{p-e}{RT} + 0.622 \frac{e}{RT} \\ \rho &= \frac{p}{RT} \left(1 - 0.378 \frac{e}{p}\right) \end{aligned} \quad (1.9)$$

This equation shows that moist air is lighter than dry air at the same temperature and pressure, for water vapour is lighter than the air it replaces.

According to equation (1.4) moisture content **or** specific humidity

$$q = \frac{d_v}{d_a + d_v}$$

Expressing it in terms of easily measurable quantities, we have, substituting for  $d_v$  and  $d_a$

$$q = \frac{0.622e}{p-0.378e} \quad \text{g/g} \quad (1.10)$$

For ordinary values of the vapour pressure,  $q$  can be

$$\text{expressed as } q = \frac{0.622e}{P} \quad \text{g/g} \quad (1.11)$$

without appreciable error.

The specific humidity at saturation pressure  $q_s$  is

$$\text{written as } q_s = \frac{0.622e_s}{p-0.378e_s} \quad (1.12)$$

### 1.3 Techniques of measurement of water vapour in the atmosphere

Unlike atmospheric pressure and temperature, measurement of humidity is one of the least satisfactory of instrumental procedures in meteorology and it is a field in which great opportunities still exist for research and invention, particularly for

measurements at very low temperatures and at very low humidities.

Routine measurements of water **vapour** at meteorological observatories are made with psychrometers, hair hygrometers or electrical capacitance and conductivity sensors to obtain surface humidities; and frost point hygrometers, infrared absorption spectrometers or electric hygrometers, using aircraft and balloons as observing platforms, to obtain **humidities** in the upper atmosphere.

The methods for measurement of air humidity fall into six main classes:

- i) Psychrometry
- ii) Dew point hygrometry
- iii) Electric hygrometry
- iv) Spectroscopic hygrometry
- v) **Coulometric** hygrometry, and
- vi) Methods using the change in dimensions, weight **etc.** of organic hygroscopic substances such as human hair, gold beater's skin etc.

A number of other sensors such as thermal conductivity cells, piezoelectric sorption hygrometers, liquid film hygrometers, capacitive humidity sensors and self-heating **phase transition hygrometers**, (the **most**

common being **lithium** chloride heated electrical hygrometers or dewcells) have also been developed and some are in regular use. Other recent developments of interest related to humidity transducers using **aluminium oxide**, barium fluoride and piezoelectric crystals.

Reliable measurements of water vapour up to about 15 km have been made from aircraft using absorption hygrometers employing the  $6.3 \mu$  absorption band of water vapour. The dew or frost point hygrometer has been found **satisfactory** to greater heights and low temperatures. It has also the great practical advantage that it needs only a very simple calibration (**Dobson** and Brewer, 1951).

The measurements which have so far been made in the atmosphere show that wide variations of relative humidity occur in the atmosphere and any relative humidity between 30 and 90 per cent is common, with large diurnal variations at the ground. Relative humidities of about 5 per cent are relatively infrequent and the lowest which has yet been observed is 0.65 per cent at **266°K** and a frost-point temperature of **219°K**. The stratosphere is found to be extremely dry with relative humidities of the order of 2 to 3 per cent over ice. The commonly observed

existence of **cirrus** layers at the tropical **tropopause** level point to substantially saturated air at and immediately below the tropopause.

In the tropopause, the water vapour distribution is extraordinarily **complex**. The atmosphere can be very moist, very dry or very variable with intense stratification. The structure of the water vapour distribution presumably arises from the complex dynamic movements which occur in the atmosphere and these are too poorly understood at present to permit a clear explanation of any particular observed distribution.

#### 1.4 Precipitable water in the atmosphere and its measurement

##### 1.4.1 Definition

If we consider an air column of **cross-sectional** area of  $1 \text{ cm}^2$ , the total mass of water vapour  $W$  contained between the height 0 and the height  $z$  would be:

$$W = \int_0^z d_v \cdot dz \quad (1.13)$$

where  $d_v$  is the vapour density or absolute humidity.

Substituting for the hydrostatic equation  $dp = -\rho g \cdot dz$

where  $\rho = d_v + d_a$  is the total air density, we have:

$$\begin{aligned}
 W &= \int_p^{p_0} \frac{dv}{\rho} \cdot \frac{1}{g} \cdot dp \\
 &= \frac{1}{g} \int_p^{p_0} q \cdot dp \quad (1.14)
 \end{aligned}$$

where  $q$  is the **specific** humidity defined as  $\frac{m_v}{m_v + m_a}$ . This can be integrated in steps or by making a plot of the specific humidity against **pressure** and finding the area between the plotted curve and  $q = 0$  and the lines  $p$  and  $p_0$ .

It is, however, simpler to express the quantity in terms of **vapour pressure** and pressure. Since  $q = 0.622 e/p$  approximately, vide equation (1.11)

$$\begin{aligned}
 W &= \frac{0.622}{g} \int_p^{p_0} e \frac{dp}{p} \\
 W &= \frac{0.622}{g} \int_p^{p_0} e \cdot d(\ln p) \quad (1.15)
 \end{aligned}$$

$W$  is the precipitable water in **grammes** per square **centimetre** of area. The last integral can be obtained graphically or integrated using a computer. It is commonly reported **as** the height at which the liquid would stand if it were completely condensed in a vessel of the same unit cross-section as the air column. Since the density of liquid water is 1, a height of 1 cm corresponds to 1  $\text{gm.cm}^{-2}$  precipitable water.

#### 1.4.2 Measurement of precipitable water

A number of techniques have been developed during the last few decades, for the measurement of computation of precipitable water in the atmosphere.

The most commonly used method of measurement is that using the selective absorption of infrared radiation by water vapour. The instrument is either located at the ground using the sun as the source or on satellites, when the upwelling radiation from the earth is used **as** the source. In both cases, measurements are made of the intensity of infrared radiation in two adjacent regions of the spectrum, one in a water vapour absorption region and the other, where no water vapour absorption occurs. The ratio of the intensities enable the precipitable water in the path

of the radiation to be calculated. A second method is the use of selective absorption in the microwave region of the spectrum. In the present study, both these methods were used. The infrared spectral hygrometer and microwave radiometer designed and constructed by the author, their principles of construction and operation, their calibration and measurement, the accuracy and sources of error and the results obtained are described in detail in Chapters 3 and 4.

#### 1.4.3 Computation of precipitable water

The most simple and direct method for the computation of precipitable water in the atmosphere is by integration from radiosonde measurements of absolute humidity in the atmosphere. A second method earlier used and later abandoned is the estimation of total precipitable water using an empirical relationship between surface water vapour pressure values and the precipitable water in the atmosphere. The radiosonde method was used in the present study to calibrate the infrared spectral hygrometer and microwave radiometer observations. Both methods of computation are **described** in ~~Chapter~~ 2 and their advantages and **disadvantages reviewed**.

#### 1.5 Purpose of the study

The original motivation for undertaking the present



study **was** the evaluation of two sites as locations suitable for a millimetre wave radioastronomical telescope. The most important factor determining the suitability of a site for ground-based observations in the millimetre wavelength range  $300\mu$  to  $3\text{mm}$ , is the attenuation by absorption and scattering of the radiation caused by more or less **constant** components of dry air, and the variable amounts of precipitable water in the atmosphere. The amount of excess attenuation and refraction **depends** on the distribution of water vapour along the path of propagation, and for the stratified atmosphere and for the skew rays the most reliable correlator for evaluation and predictions of the propagation **properties** seems to be the amount of water vapour measured at the observation site. Statistics of the amount and variation of zenithal  $W$  are therefore of importance for infrared and short wavelength radio astronomy, satellite communication and long range propagation **studies** in general.

The two sites provisionally chosen for the location of the radioastronomical telescope were Bangalore (Lat.  $12^{\circ} 58'N$ , Long.  $77^{\circ} 35'E$  950 metres **a.m.s. l**) and Nandi Hills (Lat.  $13^{\circ} 22'N$  Long.  $77^{\circ} 41'E$ , 1479 metres **a.m.s. l**). Bangalore **is** centrally located

on the Mysore plateau, about 300 km from the sea both to the east and the west, Nandi Hills, being a small hill station about 56 km north of Bangalore. Both have a ealubrioua and equable climate, Nandi Hills being naturally cooler and drier due to its higher elevation.

The four months from December to March are generally dry. April and May are characteriaed by thunderstorm activity, mostly in the afternoons and evenings. The remaining six months experience clou-  
diness and rain, as a result of the south-west monsoon from June to September and the north-east monsoon during October and November.

The present thesis describes the infrared spectral hygrometer and microwave water vapour radiometer designed and constructed by the author for the measurement of precipitable water in the atmosphere. The results of these measurements and the computation of precipitable water from radiosonde data are presented at two stations over a period of four years, providing the first detailed study of the kind for these latitudes. The relative advantages and disadvantages of each method based on long-term intercomparisons between different instru-

ments and techniques are also assessed. The results, apart from being of interest to radioastronomers, meteorologists and communication engineers dealing with microwave propagation of the atmosphere, provide invaluable ground truth measurements for verification of satellite derived data on precipitable water.

### LIST OF SYMBOLS USED

- $d_a$  - density of dry air
- $d_v$  - absolute humidity or water vapour density
- $e$  - **vapour** pressure of water vapour
- saturation vapour pressure over water
- $e_i$  - saturation vapour pressure over ice
- $m_a$  - mass of dry air
- $m_v$  - mass of water vapour
- $P$  - atmospheric pressure
- $q$  - moisture content or specific humidity
- $r$  - water vapour mixing ratio
- $r_w$  - saturation mixing ratio at the pressure and temperature of the moist air
- $R^*$  - universal **gas** content
- $T$  - temperature
- $T_d$  - thermodynamic dew point temperature
- $T_f$  - thermodynamic frost point temperature
- $V$  - volume occupied by mixture of water vapour and dry air
- $U_w$  - relative humidity with respect to water of **moist** air
- $T_w$  - thermodynamic wet bulb temperature
- $\rho$  - density of moist air

LIST OF FIGURES

- 1.1 Water vapour absorption in the various regions of solar and terrestrial radiation spectra.

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